

Polynomials – CBSE Class 10 Mathematics/Previous Year Question Paper Questions & Answers/Model Questions

1. If α and β are zeros of the quadratic polynomial $f(x) = x^2 - x - 4$, then what is the value of $\frac{1}{\alpha} + \frac{1}{\beta} - \alpha\beta$?

Answer:

$$\alpha + \beta = 1, \alpha\beta = -4$$

$$\text{Now } \frac{1}{\alpha} + \frac{1}{\beta} - \alpha\beta = \frac{\alpha + \beta}{\alpha\beta} - \alpha\beta = \frac{1}{-4} - (-4) = \frac{-1}{4} + 4 = \frac{15}{4}$$

2. What is the value of x , for which the polynomials $x^2 - 1$ and $x^2 - 2x + 1$ vanish simultaneously.

Answer:

$$x^2 - 1 = (x - 1)(x + 1)$$

$$x^2 - 2x + 1 = (x - 1)(x - 1)$$

Both have $x = 1$ as zero, so both vanish if $x = 1$

3. If one zero of the polynomial $3x^2 + 8x + k$ is the reciprocal of the other, then what is the value of k ?

Answer:

Let the zeroes be α and $\frac{1}{\alpha}$

$$\text{Product of zeroes} = \alpha \times \frac{1}{\alpha} = \frac{k}{3}$$

$$k = 3$$

4. If one of the zeroes of the quadratic polynomial $(k-1)x^2 + kx + 1$ is -3 , then what is the value of k ?

Answer:

If -3 is a zero of the polynomial $p(-3) = 0$

$$(k - 1)(-3)^2 + k(-3) + 1 = 0$$

$$(k - 1)9 - 3k + 1 = 0$$

$$9k - 9 - 3k + 1 = 0$$

$$6k - 8 = 0$$

$$k = \frac{8}{6} = \frac{4}{3}$$

5. If one zero of the quadratic polynomial $x^2 + 3x + k$ is 2, then what is the value of k ?

Answer:

Let $p(x) = x^2 + 3x + k$

If 2 is a zero of $p(x)$, $p(2) = 0$

$$p(2) = 2^2 + 3 \times 2 + k = 0$$

$$4 + 6 + k = 0$$

$$10 + k = 0$$

$$k = -10$$

6. If one zero of a quadratic polynomial $kx^2 + 3x + k$ is 2, then what is the value of k ?

Answer:

Since 2 is a zero of the quadratic polynomial, $p(2) = 0$

$$k(2^2) + 3 \times 2 + k = 0$$

$$4k + 6 + k = 0$$

$$5k + 6 = 0$$

$$5k = -6$$

$$k = \frac{-6}{5}$$

7. If α and β are the zeros of the polynomial $2x^2 - 13x + 6$, then what is the value of $\alpha + \beta$?

Answer:

$$\alpha + \beta = \frac{-b}{a} = \frac{-(-13)}{2} = \frac{13}{2}$$

8. If the sum of the zeroes of the quadratic polynomial $kx^2 + 2x + 3k$ is equal to their product, then what is the value of k ?

Answer:

Let the zeroes be α and β .

$$\alpha + \beta = \frac{-2}{k}$$

$$\alpha\beta = \frac{3k}{k} = 3$$

$$\alpha + \beta = \alpha\beta \text{ (given)}$$

$$\frac{-2}{k} = 3$$

$$k = \frac{-2}{3}$$

9. Find the quadratic polynomial, the sum of whose zeroes is -5 and their product is 6.

Answer:

Let the zeroes be α and β

$$\text{Given } \alpha + \beta = -5$$

$$\alpha\beta = 6$$

Required quadratic polynomial is $x^2 - (\alpha + \beta)x + \alpha\beta$

$$= x^2 - (-5x) + 6 = x^2 + 5x + 6$$

10. If the sum and product of the zeroes of a quadratic polynomial are 3 and -10 respectively, find the quadratic polynomial?

Answer:

$x^2 - (\alpha + \beta)x + \alpha\beta = x^2 - 3x - 10$, which is the required quadratic polynomial.
